

Funktionen

- konstant
- linear
- quadratisch
- ganz-rational

$\frac{p}{q}$

- gebrochen-rational (Wurzel)

$x \rightarrow y$

$$f(x) = ax^0 = z$$

$$f(x) = ax + b = \frac{1}{2}x + 2$$

$$f(x) = ax^2 + bx + c = 2x^2 - 3x + 1$$

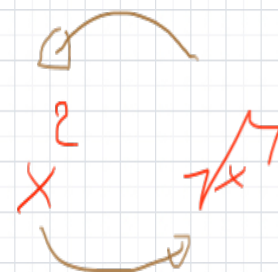
$$f(x) = ax^n + bx^{n-1} + \dots + wx^0 \quad n = \text{Grad!}$$

$$f(x) = ax^{\frac{1}{2}}$$

$$f(x) = x^{\frac{3}{4}}$$

$$f(x) = x^{\frac{1}{2}} = \sqrt{x}$$

$$= (x^{\frac{1}{2}})^2 = x^{\frac{1}{2} \cdot 2} = x^1$$



- Exp./Log-Funktion

$$f(x) = a^x$$

- Trigonometrisch

$$f(x) = \underline{e^x} \quad f'(x) = \underline{e^x}$$

$$f(x) = \sin / \cos / \tan \dots x$$

Funktionen verbinden

/ ableiten

$$u(x) = x^2$$

$$v(x) = 3e^x$$

$$u + v$$

$$\underbrace{x^2} + \underbrace{3e^x}$$

$$2x + 3e^x$$

$$u - v$$

$$x^2 - 3e^x$$

$$2x - 3e^x$$

$$\underline{u \cdot v}$$

$$x^2 \cdot 3e^x$$

$$\underline{u : v} = \frac{u}{v}$$

$$\frac{x^2}{3e^x}$$

$$u(v)$$

$$(3e^x)^2$$

$$v(u)$$

$$3e^{(x^2)}$$

Produktregel

$$f(x) = u \cdot v$$

$$f'(x) = u'v + u \cdot v'$$

Quotientenregel

$$f(x) = \frac{u}{v}$$

$$f'(x) = \frac{u'v - uv'}{v^2}$$

Kettenregel

$$f(x) = u(v(x))$$

$$f'(x) = v'(x) \cdot u'(v)$$

↓

$$u \quad v$$

$$x^2 \cdot 3e^x$$

$$\frac{x^2}{3e^x}$$

$$(3e^x)^2$$

$$3e^{(x^2)}$$

u'/v

$$u' = 2x$$

$$v' = 3e^x$$

f'

$$f'(x) = 2x \cdot 3e^x + x^2 \cdot 3e^x$$

$$= (6x + 3x^2) \cdot e^x$$

$$f'(x) = \frac{2x \cdot 3e^x - x^2 \cdot 3e^x}{(3e^x)^2} = \frac{(2x - x^2) \cdot 3e^x}{(3e^x)^2}$$

$$f'(x) = (3e^x) \cdot 2 \cdot (3e^x)^{-1} = 2 \cdot (3e^x)^2 = 18e^{2x}$$

$$f'(x) = 2x \cdot 3e^{x^2} = 6x \cdot e^{x^2}$$

Integrale / Integrieren

$$f'(x) = \frac{1}{2} \cdot x + 2$$

$$f(x) = \frac{1}{4} x^2 + 2x$$
$$F(x) = \frac{1}{3} \cdot \frac{1}{4} x^3 + x^2$$



